

# Private Authentication with Alpha-Beta Privacy

**Laouen Fernet**    Sebastian Mödersheim

DTU Compute  
{lpkf, samo}@dtu.dk

June 15, 2023

# Increasing digitalization

---



Health



Payment



Transport



Voting

- Strong guarantees of privacy
- More subtle than secrecy

# Alpha-Beta Privacy

---

- Declarative and intuitive, based on logic
- Payload  $\alpha$
- Technical information  $\beta$
- Tool support

$$\alpha \equiv \text{age} \geq 18 \quad \alpha \equiv v_1, \dots, v_n \in \{0, 1\} \wedge \sum_{i=1}^n v_i = 42$$

Unlinkability:  $x_1, \dots, x_n \in \text{Tags}$

# This Paper

---

- New specifications for BAC and Private Authentication
- Discussion of modeling challenges
- Explanation of the tool output

# Passport Reader

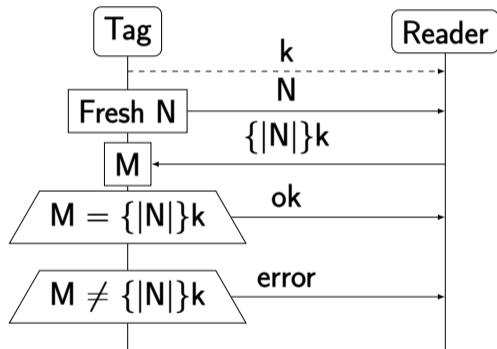
---



CBP International Travel Preclearance Operations in Canada, U.S. Customs and Border Protection, public domain

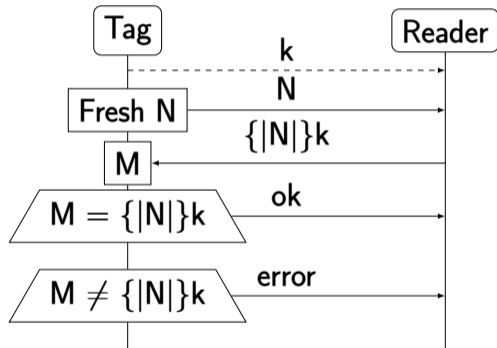
# BAC: Challenge

---



# BAC: Challenge

---



Transaction Challenge:

\* Tag in  $\{t1, t2\}$ .

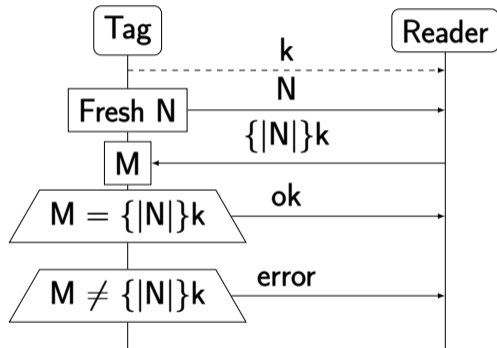
**new** Nonce.

**send** session (Tag, Nonce).

**send** Nonce.

**send**  $\text{scrypt}(\text{sk}(\text{Tag}), \text{Nonce})$

# BAC: Response



Transaction Response:

**receive** Session.

**try** Tag = sfst(Session) **in**

**try** Nonce = ssnd(Session) **in**

**receive** M.

**try**

    N = dscrypt(sk(Tag),M)

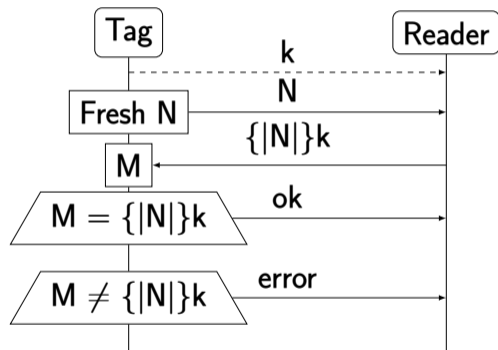
**in**

...



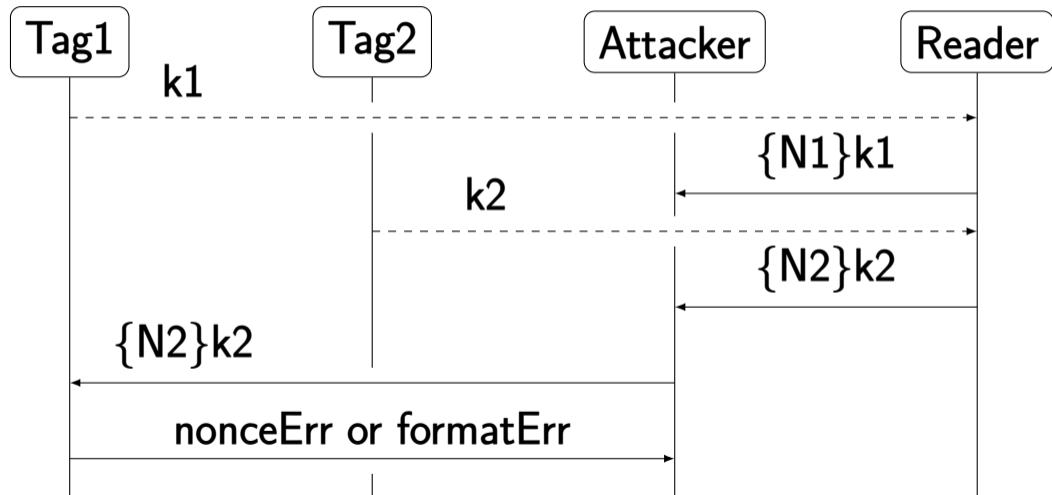
# BAC: Response

---



```
...  
State := noncestate [Nonce].  
if Nonce = N and  
    State = fresh then  
    noncestate [N] := spent.  
    send ok  
else send nonceErr  
catch send formatErr
```

# BAC: Attack Trace $\text{Tag1} \stackrel{?}{=} \text{Tag2}$



# BAC: Attack Trace

Tag1  $\stackrel{?}{=} \text{Tag2}$

---

2 Challenge transactions:  $\alpha \equiv \text{Tag1}, \text{Tag2} \in \{t1, t2\}$

l1  $\mapsto \text{session}(\text{Tag1}, \text{Nonce1})$     l2  $\mapsto \text{scrypt}(\text{sk}(\text{Tag1}), \text{Nonce1})$

l3  $\mapsto \text{session}(\text{Tag2}, \text{Nonce2})$     l4  $\mapsto \text{scrypt}(\text{sk}(\text{Tag2}), \text{Nonce2})$

# BAC: Attack Trace $\text{Tag1} \stackrel{?}{=} \text{Tag2}$

---

2 Challenge transactions:  $\alpha \equiv \text{Tag1}, \text{Tag2} \in \{t1, t2\}$

$l1 \mapsto \text{session}(\text{Tag1}, \text{Nonce1})$      $l2 \mapsto \text{sCrypt}(\text{sk}(\text{Tag1}), \text{Nonce1})$

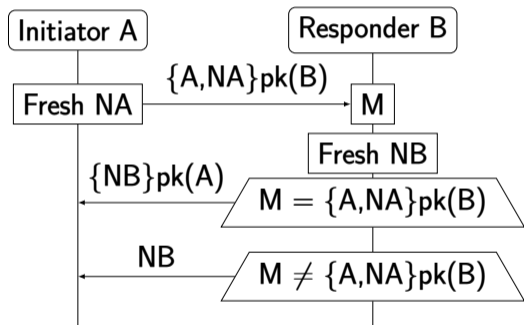
$l3 \mapsto \text{session}(\text{Tag2}, \text{Nonce2})$      $l4 \mapsto \text{sCrypt}(\text{sk}(\text{Tag2}), \text{Nonce2})$

The intruder uses session  $l1$  but encryption  $l4$ :

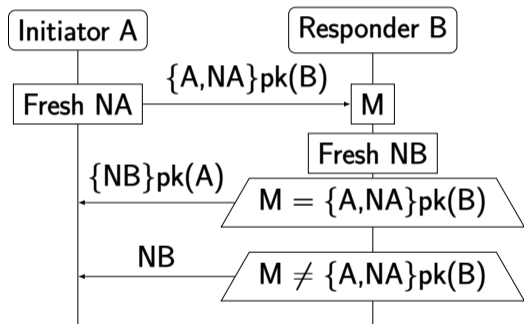
- decryption works iff  $\text{Tag1} = \text{Tag2}$
- `nonceErr` if  $\text{Tag1} = \text{Tag2}$
- `formatErr` if  $\text{Tag1} \neq \text{Tag2}$

# AF0: Initiator

---



# AF0: Initiator



Transaction Initiator:

\*  $A$  in  $\{a, b\}$ .

\*  $B$  in  $\{a, b, i\}$ .

**if**  $B = i$  **then new**  $NA, R$ .

**send**  $\text{crypt}(pk(B),$   
 $\text{pair}(A, NA), R)$ .

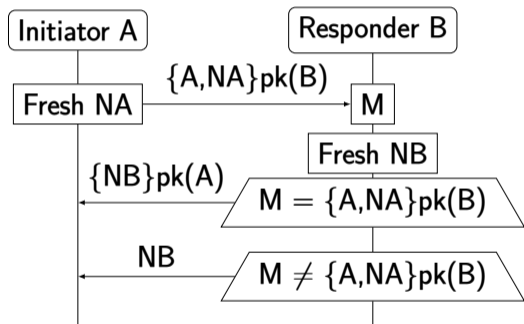
\*  $A = \text{gamma}(A)$  and  
\*  $B = \text{gamma}(B)$

**else new**  $NA, R$ .

**send**  $\text{crypt}(pk(B),$   
 $\text{pair}(A, NA), R)$ .

\*  $B$  in  $\{a, b\}$

# AF0: Responder



Transaction Responder:

\* B in {a, b}.

**receive** M.

**try**

DEC = dcrypt(inv(pk(B)), M)

A = proj1(DEC) **in**

**if** A = i **then new** NB, R.

**send** crypt(pk(A), NB, R).

\* B = gamma(B)

**else new** NB, R.

**send** crypt(pk(A), NB, R)

**catch new** NB. **send** NB

# AF0: Attack Trace

---

In the paper :)



# Conclusions

---

- $(\alpha, \beta)$ -privacy for real protocols: declarative, intuitive
- Rediscovery of attacks and better understanding of privacy guarantees
- Useful to find strongest goal